

**DERIVADAS**

1.  $y = 5x^6 - 3x^5 + 3x^3 - 2$
2.  $y = x^{-4} + 2x^{-3} + x - 4$
3.  $y = 3x^{10} + 2\sqrt{x} + \frac{3}{x}$
4.  $y = \sqrt{3} \cdot x^3 - p \cdot x + \sqrt{3}$
5.  $y = 4 \operatorname{sen} x - 3 \operatorname{cos} x$
6.  $y = 2\sqrt{x} + \frac{2}{x} + x^5$
7.  $y = 4x^3 + 2x^3 - x^3 + 4$
8.  $y = \frac{p}{2} \cdot \cos x - 3\sqrt{x}$
9.  $y = \cos(3x)$
10.  $y = \cos^2(x^3)$
11.  $y = \operatorname{sen}(3x^2 - 2x)$
12.  $y = \cos(x^2)$
13.  $y = \operatorname{sen}^3(2x^2)$
14.  $y = \cos^4(3x^4)$
15.  $y = 3 \operatorname{sen}^2(2x - 3)$
16.  $y = \cos^5(3x^2)$
17.  $y = \cos(\operatorname{sen} x)$
18.  $y = \cos^2(\operatorname{sen}(3x))$
19.  $y = \sqrt[3]{\cos^2 x}$
20.  $y = \sqrt[3]{\cos^2(x^2)}$
21.  $y = \sqrt{x^2 - 3x}$
22.  $y = \sqrt[3]{(x^2 - 3x)^2}$
23.  $y = (2\sqrt{x} - 3x)^3$
24.  $y = \sqrt[3]{\operatorname{sen}^2 x}$
25.  $y = \sqrt[3]{\operatorname{sen}(3x)}$
26.  $y = \sqrt{3x - \operatorname{sen} x}$
27.  $y = (3x^2 - \sqrt{1 - x^2})^3$
28.  $y = \operatorname{sen}(\sqrt{3x^2 - 5x})$
29.  $y = \sqrt{\operatorname{sen}^3 x + (x - 1)^3}$
30.  $y = \cos^3(x^2 - 3\sqrt{x})$
31.  $y = \frac{x}{5}$
32.  $y = \frac{5}{x}$
33.  $y = \frac{x^4 - 3x}{4}$
34.  $y = \frac{x^3 - 3}{x}$
35.  $y = \frac{(x^4 - 3x)^2}{3}$
36.  $y = \frac{(x - 1)^3}{3x}$
37.  $y = \frac{x^2}{x^2 - 1}$
38.  $y = \frac{\sqrt{3x}}{x}$
39.  $y = \sqrt{\frac{3}{x}}$
40.  $y = \frac{x}{\sqrt{3x}}$
41.  $y = \sqrt[3]{3x^2 - \operatorname{sen} x}$
42.  $y = \ln(3x - 1)$
43.  $y = \ln(x^2 - 3x)$
44.  $y = \ln\sqrt{x - 2}$
45.  $y = \log_2(3x^2)$
46.  $y = e^{x^2}$
47.  $y = 2^x$
48.  $y = e^{x^2 - 2x}$
49.  $y = 3^{\operatorname{sen} x}$
50.  $y = \operatorname{tg}(x^3)$
51.  $y = 3e^{x^2 - 3x}$
52.  $y = \sqrt{e^{\operatorname{cos} x}}$
53.  $y = 3 \operatorname{tg}^2 x$
54.  $y = (x^2 - 1) \cdot (x - 1)$
55.  $y = x^2 \cdot \ln x$
56.  $y = e^{x^2} \cdot \cos x$
57.  $y = x^4 \cdot e^{3x}$
58.  $y = e^{x^4 - 3x^2} \cdot \operatorname{sen} x$

59.  $y = \ln x^2 \cdot e^{\sin x}$

61.  $y = \left( \frac{x^2 - 3}{x^2 + 1} \right)^3$

63.  $y = (\cos^2 3x - \sin^3 x) \cdot e^{x^3}$

65.  $y = \frac{\ln x}{3^x}$

67.  $y = \ln \left( \frac{\sin x}{e^x} \right)$

69.  $y = \frac{3x^4 - 2x^2 + 3x - 2}{2x - 1}$

71.  $y = \arctg(x^2)$

73.  $y = \ln(\sec x)$

75.  $y = \arcsen x \cdot e^{\cos x}$

77.  $y = \ln \left( \frac{\operatorname{tg} x}{e^{3x^2}} \right)$

79.  $y = \ln(\arctg(5x))$

81.  $y = 5 \arctg^2(\sin x)$

83.  $y = \frac{\arcsen(3x - 2)}{x^2}$

85.  $y = x^{\sin x}$

87.  $y = (\cos x)^{x^2 - x}$

89.  $y = \ln \left( \frac{x + 2}{x^2} \right)^3$

91.  $y = 10 \left( \frac{\sin x - e^x}{3x - \cos x} \right)$

93.  $y = \frac{x^{\cos x}}{(\ln x)^3}$

95.  $y = \sqrt[3]{\frac{\sin^2(e^x)}{\arctg(\cos x)}}$

97.  $y = \frac{\sqrt{\cos(e^x) \cdot x}}{\sqrt{e^{\operatorname{tg} x}}}$

99.  $y = \sqrt{\frac{\arctg e^x \cdot \cos x}{\ln(x^2 - x)}}$

60.  $y = \frac{1}{\ln \sqrt{x}}$

62.  $y = \ln x \cdot e^{x^2 - \sin x}$

64.  $y = \left( \frac{\ln x^2}{x^3 - 2} \right)^2$

66.  $y = \frac{e^x + \ln x}{x^2 - \sin x}$

68.  $y = \sqrt{\frac{\sin x}{x - 1}}$

70.  $y = (\sin(e^{3x}))^2 \cdot \cos x$

72.  $y = \arcsen x^3$

74.  $y = \arctg(\ln x)$

76.  $y = \arctg(e^{3x})$

78.  $y = \arcsen \left( \frac{x + 1}{e^x} \right)$

80.  $y = \arctg \sqrt{x^3}$

82.  $y = 3^{\arctg(x^2)}$

84.  $y = \frac{\sin x - \operatorname{tg} x}{\sqrt{4x - 3}}$

86.  $y = (\sin x)^{x^2}$

88.  $y = 4^{\arctg(\ln x)}$

90.  $y = \left( \frac{e^{3x}}{\sin x} \right)^{x^2}$

92.  $y = \cos \left( \frac{\operatorname{tg} \sqrt{x}}{\sin(\ln x)} \right)$

94.  $y = \cos^2(4e^x) \cdot \ln \left( \frac{\operatorname{tg} x}{3^{x^2}} \right)$

96.  $y = \sqrt{\frac{e^{\ln(\cos x)}}{5^{\cos x}}}$

98.  $y = (\operatorname{tg}(e^x) + x^2)^x$

100.  $y = \frac{\ln \sqrt{\cos x}}{\sin(e^{\cos x})}$

**SOLUCIONES**

Todas las soluciones se dan sin simplificar

1.  $y' = 30x^5 - 15x^4 + 9x^2$
2.  $y' = -4x^{-5} - 6x^{-4} + 1$
3.  $y' = 30x^9 + \frac{1}{\sqrt{x}} - \frac{3}{x^2}$
4.  $y' = 3\sqrt{3} \cdot x^2 - \mathbf{P}$
5.  $y' = 4 \cos x + 3 \operatorname{sen} x$
6.  $y' = \frac{1}{\sqrt{x}} - \frac{2}{x^2} + 5x^4$
7.  $y' = 15x^2$
8.  $y' = -\frac{\mathbf{P}}{2} \operatorname{sen} x - \frac{3}{2\sqrt{x}}$
9.  $y' = -3 \operatorname{sen}(3x)$
10.  $y' = -2 \cos(x^3) \cdot \operatorname{sen}(x^3) \cdot 3x^2$
11.  $y' = \cos(3x^2 - 2x) \cdot (6x - 2)$
12.  $y' = -\operatorname{sen}(x^2) \cdot 2x$
13.  $y' = 3 \operatorname{sen}^2(2x^2) \cdot \cos(2x^2) \cdot 4x$
14.  $y' = 4 \cos^3(3x^4) \cdot (-\operatorname{sen}(3x^4)) \cdot 12x^3$
15.  $y' = 6 \operatorname{sen}(2x - 3) \cdot \cos(2x - 3) \cdot 2$
16.  $y' = 5 \cos^4(3x^2) \cdot (-\operatorname{sen}(3x^2)) \cdot 6x$
17.  $y' = -\operatorname{sen}(\operatorname{sen} x) \cdot \operatorname{cos} x$
18.  $y' = 2 \cos(\operatorname{sen} 3x) \cdot (-\operatorname{sen}(\operatorname{sen} 3x)) \cdot \cos 3x \cdot 3$
19.  $y' = \frac{-2 \operatorname{cos} x \cdot \operatorname{sen} x}{3 \sqrt[3]{\cos^4 x}}$
20.  $y' = \frac{-2 \cos(x^2) \cdot \operatorname{sen}(x^2) \cdot 2x}{3 \sqrt[3]{\cos^4(x^2)}}$
21.  $y' = \frac{2x - 3}{2 \sqrt{x^2 - 3x}}$
22.  $y' = \frac{2(x^2 - 3x)(2x - 3)}{3 \sqrt[3]{(x^2 - 3x)^4}}$
23.  $y' = 3 \left( 2\sqrt{x} - 3x \right)^2 \cdot \left( \frac{1}{\sqrt{x}} - 3 \right)$
24.  $y' = \frac{2 \operatorname{sen} x \operatorname{cos} x}{3 \sqrt[3]{\operatorname{sen}^4 x}}$
25.  $y' = \frac{3 \operatorname{cos} 3x}{5 \sqrt[5]{\operatorname{sen}^4(3x)}}$
26.  $y' = \frac{3 - \operatorname{cos} x}{2 \sqrt{3x - \operatorname{sen} x}}$
27.  $y' = 3 \left( 3x^2 - \sqrt{1 - x^2} \right)^2 \cdot \left( 6x - \frac{-2x}{2\sqrt{1 - x^2}} \right)$
28.  $y' = \cos \left( \sqrt{3x^2 - 5x} \right) \cdot \frac{6x - 5}{2\sqrt{3x^2 - 5x}}$
29.  $y' = \frac{3 \operatorname{sen}^2 x \operatorname{cos} x + 3(x - 1)^2}{2 \sqrt{\operatorname{sen}^3 x + (x - 1)^3}}$
30.  $y' = -3 \cos^2(x^2 - 3\sqrt{x}) \cdot \operatorname{sen}(x^2 - 3\sqrt{x}) \cdot \left( 2x - \frac{3}{2\sqrt{x}} \right)$
31.  $y' = \frac{1}{5}$
32.  $y = -\frac{5}{x^2}$
33.  $y' = \frac{4x^3 - 3}{4}$
34.  $y' = 2x + \frac{3}{x^2}$
35.  $y' = \frac{2(x^4 - 3x)^2 \cdot (4x^3 - 3)}{3}$
36.  $y' = \frac{3(x - 1)^2 \cdot 3x - 3(x - 1)^3}{(3x)^2}$
37.  $y' = \frac{2x(x^2 - 1) - x^2 \cdot 2x}{(x^2 - 1)^2}$
38.  $y' = \frac{3}{2\sqrt{3x}} \cdot x - \sqrt{3x}$

- $$39. y' = \frac{1}{2\sqrt{\frac{3}{x}}} \cdot \frac{-3}{x^2}$$
- $$40. y' = \frac{\sqrt{3x} - x \frac{3}{2\sqrt{3x}}}{3x}$$
- $$41. y' = \frac{6x - \cos x}{3\sqrt[3]{(3x^2 - \sin x)^2}}$$
- $$42. y' = \frac{3}{3x-1}$$
- $$43. y' = \frac{2x-3}{x^2-3x}$$
- $$44. y' = \frac{1}{2\sqrt{x-2}} \cdot \frac{1}{\sqrt{x-2}}$$
- $$45. y' = \frac{6x}{3x^2 \cdot \ln 2}$$
- $$46. y' = e^{x^2} \cdot 2x$$
- $$47. y' = 2^x \cdot \ln 2$$
- $$48. y' = e^{x^2-2x} \cdot (2x-2)$$
- $$49. y' = 3^{\sin x} \cdot \cos x \cdot \ln 3$$
- $$50. y' = \frac{3x^2}{\cos^2(x^3)}$$
- $$51. y' = 3 e^{x^2-3x} \cdot (2x-3)$$
- $$52. y' = \frac{-e^{\cos x} \sin x}{2\sqrt{e^{\cos x}}}$$
- $$53. y' = \frac{6 \operatorname{tg} x}{\cos^2 x}$$
- $$54. y = 2x(x-1) + (x^2-1)$$
- $$55. y' = 2x \cdot \ln x + \frac{x^2}{x}$$
- $$56. y' = e^{x^2} 2x \cos x - e^{x^2} \sin x$$
- $$57. y' = 4x^3 \cdot e^{3x} + x^4 e^{3x} \cdot 3$$
- $$58. y' = e^{x^4-3x^2} \cdot (4x^3-6x) \sin x + e^{x^4-3x^2} \cos x$$
- $$59. y' = \frac{2x}{x^2} \cdot e^{\sin x} + \ln x^2 e^{\sin x} \cos x$$
- $$60. y' = \frac{1}{\frac{2\sqrt{x}}{\sqrt{x}} \cdot \frac{1}{(\ln \sqrt{x})^2}}$$
- $$61. y' = 3 \left( \frac{x^2-3}{x^2+1} \right)^2 \cdot \frac{2x(x^2+1) - (x^2-3)2x}{(x^2+1)^2}$$
- $$62. y' = \frac{1}{x} \cdot e^{x^2-\sin x} + \ln x \cdot e^{x^2-\sin x} (2x - \cos x)$$
- $$63. y' = (2 \cos 3x (-\sin 3x) 3 - 3 \sin^2 x \cos x) \cdot e^{x^3} + (\cos^2 3x - \sin^3 x) e^{x^3} 3x^2$$
- $$64. y' = 2 \left( \frac{\ln x^2}{x^3-2} \right) \cdot \frac{\frac{2x}{x^2} (x^3-2) - \ln x^2 3x^2}{(x^3-2)^2}$$
- $$65. y' = \frac{\frac{1}{x} 3^x - \ln x 3^x \ln 3}{(3^x)^2}$$
- $$66. y' = \frac{\left( e^x + \frac{1}{x} \right) (x^2 - \sin x) - (e^x + \ln x) (2x - \cos x)}{(x^2 - \sin x)^2}$$
- $$67. y' = \frac{e^x \cos x e^x - e^x \sin x}{\sin x (e^x)^2}$$
- $$68. y' = \frac{1}{2\sqrt{\frac{\sin x}{x-1}}} \cdot \frac{\cos x (x-1) - \sin x}{(x-1)^2}$$

$$69. y' = \frac{(12x^3 - 4x + 3)(2x - 1) - (3x^4 - 2x^2 + 3x - 2) \cdot 2}{(2x - 1)^2}$$

$$70. y' = 2 \left( \operatorname{sen}(e^{3x}) \right) \cdot \cos(e^{3x}) \cdot e^{3x} \cdot 3 \cos x - \left( \operatorname{sen}(e^{3x}) \right)^2 \cdot \operatorname{sen} x$$

$$71. y' = \frac{2x}{1 + x^4}$$

$$72. y' = \frac{3x^2}{\sqrt{1 - x^6}}$$

$$73. y' = \frac{\frac{\operatorname{sen} x}{\cos^2 x}}{\sec x}$$

$$74. y' = \frac{\frac{1}{x}}{1 + (\ln x)^2}$$

$$75. y' = \frac{e^{\cos x}}{\sqrt{1 - x^2}} - \operatorname{arcsen} x \cdot e^{\cos x} \operatorname{sen} x$$

$$76. y' = \frac{e^{3x} \cdot 3}{1 + (e^{3x})^2}$$

$$77. y' = \frac{e^{3x^2}}{\operatorname{tg} x} \cdot \frac{\frac{e^{3x^2}}{\cos^2 x} - \operatorname{tg} x \cdot e^{3x^2} \cdot 6x}{(e^{3x^2})^2}$$

$$78. y' = \frac{\frac{e^x - (x+1)e^x}{(e^x)^2}}{\sqrt{1 - \left( \frac{x+1}{e^x} \right)^2}}$$

$$79. y' = \frac{1}{\operatorname{arctg}(5x)} \cdot \frac{5}{1 + (5x)^2}$$

$$80. y' = \frac{\frac{3x^2}{2\sqrt{x^3}}}{1 + x^3}$$

$$81. y' = 10 \operatorname{arctg}(\operatorname{sen} x) \cdot \frac{\cos x}{1 + \operatorname{sen}^2 x}$$

$$82. y' = 3^{\operatorname{arctg}(x^2)} \cdot \frac{2x}{1 + x^4} \ln 3$$

$$83. y' = \frac{\frac{3x^2}{\sqrt{1 - (3x - 2)^2}} - \operatorname{arcsen}(3x - 2) \cdot 2x}{x^4}$$

$$84. y' = \frac{\left( \cos x - \frac{1}{\cos^2 x} \right) \sqrt{4x - 3} - (\operatorname{sen} x - \operatorname{tg} x) \cdot \frac{4}{2\sqrt{4x - 3}}}{4x - 3}$$

$$85. y' = \left( \cos x \cdot \ln x + \frac{\operatorname{sen} x}{x} \right) \cdot x^{\operatorname{sen} x}$$

$$86. y' = \left( 2x \ln(\operatorname{sen} x) + \frac{x^2 \cos x}{\operatorname{sen} x} \right) (\operatorname{sen} x)^{x^2}$$

$$87. y' = \left( (3x^2 - 1) \ln \cos x - \frac{(x^3 - x) \operatorname{sen} x}{\cos x} \right) \cdot (\cos x)^{x^3 - x}$$

$$88. y' = 4^{\operatorname{arctg}(\ln x)} \cdot \frac{\frac{1}{x}}{1 + (\ln x)^2} \cdot \ln 4$$

$$89. y' = \frac{1}{\left( \frac{x+2}{x^2} \right)^3} \cdot 3 \left( \frac{x+2}{x^2} \right)^2 \cdot \frac{x^2 - 2x(x+2)}{x^4}$$

$$90. y' = \left( 2x \ln x \left( \frac{e^{3x}}{\operatorname{sen} x} \right) + x^2 \frac{\operatorname{sen} x}{e^{3x}} \frac{3e^{3x} \operatorname{sen} x - e^{3x} \operatorname{cos} x}{\operatorname{sen}^2 x} \right) \cdot \left( \frac{e^{3x}}{\operatorname{sen} x} \right)^2$$

$$91. y' = 10 \left( \frac{\operatorname{sen} x - e^x}{3x - \operatorname{cos} x} \right) \cdot \ln 10 \frac{(\operatorname{cos} x - e^x)(3x - \operatorname{cos} x) - (\operatorname{sen} x - e^x)(3 + \operatorname{sen} x)}{(3x - \operatorname{cos} x)^2}$$

$$92. y' = -\operatorname{sen} \left( \frac{\operatorname{tg} \sqrt{x}}{\operatorname{sen}(\ln x)} \right) \cdot \frac{\frac{1}{\operatorname{cos}^2 \sqrt{x}} \cdot \frac{1}{2\sqrt{x}} \cdot \operatorname{sen}(\ln x) - \operatorname{tg} \sqrt{x} \cdot \operatorname{cos}(\ln x) \cdot \frac{1}{x}}{\operatorname{sen}^2(\ln x)}$$

$$93. y' = \frac{\left( -\operatorname{sen} x \ln nx + \frac{\operatorname{cos} x}{x} \right) x^{\operatorname{cos} x} (\ln x)^3 - x^{\operatorname{cos} x} 3 (\ln x)^2 \frac{1}{x}}{(\ln x)^6}$$

94.

$$y' = 2 \operatorname{cos}(4e^x) \cdot (-\operatorname{sen}(4e^x)) \cdot 4e^x \cdot \ln \left( \frac{\operatorname{tg} x}{3^{x^2}} \right) + \operatorname{cos}^2(4e^x) \cdot \frac{3^{x^2} \frac{3^{x^2}}{\operatorname{cos}^2 x} - \operatorname{tg} x \cdot 3^{x^2} \cdot 2x \cdot \ln 3}{(3^{x^2})^2}$$

$$95. y = \frac{1}{2 \sqrt{\frac{e^{\ln(\operatorname{cos} x)}}{5^{\operatorname{cos} x}}}} \cdot \frac{e^{\ln(\operatorname{cos} x)} \frac{-\operatorname{sen} x}{\operatorname{cos} x} \cdot 5^{\operatorname{cos} x} - e^{\ln(\operatorname{cos} x)} \cdot 5^{\operatorname{cos} x} (-\operatorname{sen} x) \ln 5}{(5^{\operatorname{cos} x})^2}$$

96.

$$y' = \frac{1}{3 \sqrt[3]{\frac{\operatorname{sen}^2(e^x)}{\operatorname{arctg}(\operatorname{cos} x)}}} \cdot \frac{2 \operatorname{sen}(e^x) \cdot \operatorname{cos}(e^x) \cdot e^x \cdot \operatorname{arctg}(\operatorname{cos} x) - \operatorname{sen}^2(e^x) \cdot \frac{1}{1 + \operatorname{cos}^2 x} \cdot (-\operatorname{sen} x)}{\operatorname{arctg}^2(\operatorname{cos} x)}$$

$$97. y' = \frac{\frac{-\operatorname{sen}(e^x) e^x x + \operatorname{cos}(e^x)}{\sqrt{\operatorname{cos}(e^x) \cdot x}} \cdot \sqrt{e^{\operatorname{tg} x}} - \sqrt{\operatorname{cos}(e^x) \cdot x} \cdot \frac{1}{2 \sqrt{e^{\operatorname{tg} x}}} \cdot e^{\operatorname{tg} x} \cdot \frac{1}{\operatorname{cos}^2 x}}{e^{\operatorname{tg} x}}$$

$$98. y' = \left( \ln(\operatorname{tge}^x + x^2) + x \frac{\frac{e^x}{\operatorname{cos}^2(e^x)} + 2x}{\operatorname{tge}^x + x^2} \right) \cdot (\operatorname{tg}(e^x) + x^2)^x$$

99.

$$y' = \frac{1}{2 \sqrt{\frac{\operatorname{arctg} e^x \cdot \operatorname{cos} x}{\ln(x^2 - x)}}} \cdot \frac{\left( \frac{e^x}{1 + (e^x)^2} \operatorname{cos} x - \operatorname{arctg} e^x \operatorname{sen} x \right) \ln(x^2 - x) - (\operatorname{arctg} e^x \operatorname{cos} x) \frac{2x - 1}{x^2 - x}}{\ln^2(x^2 - x)}$$

$$100. y' = \frac{\frac{1}{\sqrt{\cos x}} \frac{-\sin x}{2\sqrt{\cos x}} \sin(e^{\cos x}) - \ln \sqrt{\cos x} \cos(e^{\cos x}) e^{\cos x} (-\sin x)}{\sin^2(e^{\cos x})}$$