1. Resuelve: $3^{2(x+1)} - 28 \cdot 3^x + 3 = 0$

2. Resuelve: $2 \log x - 1 = \log (x^2 - 6)$

3. Resuelve: $\begin{cases} x - y = 3 \\ 2^x - 2^y = \frac{7}{4} \end{cases}$

4. Si log 2=0,3010, log 3= 0,4771, log 5= 0,6990. Calcula:

    a. $\log \sqrt[6]{\dfrac{1}{0,128}}$ b. $\log \dfrac{540}{256}$

5. Escribe la expresión algebraica de: $\log A = 2 + 5 \log x - \dfrac{3}{5} \log(y) - 4 \log z - 3 \log \dfrac{x}{y}$

6. Resuelve: $\left.\begin{array}{l} \log x - \log y = 1 \\ 3x + 2y = 64 \end{array}\right\}$

7. Resuelve $\dfrac{\log 2 + \log(11 - x^2)}{\log(5 - x)} = 2$

8. Resuelve $4^{1+x} + 2^{x+3} = 320$

① $3^{2(x+1)} - 28 \cdot 3^x + 3 = 0$

$3^{2x+2} - 28 \cdot 3^x + 3 = 0 \longrightarrow (3^x)^2 \cdot 3^2 - 28 \cdot 3^x + 3 = 0 \xrightarrow{3^x = t}$

$9t^2 - 28t + 3 = 0 \longrightarrow t = \dfrac{28 \pm \sqrt{28^2 - 4 \cdot 9 \cdot 3}}{18} = \begin{cases} 3 \\ \frac{1}{9} \end{cases}$

$t_1 = 3 \longrightarrow 3^x = 3 \longrightarrow x = 1$

$t_2 = \frac{1}{9} \longrightarrow 3^x = 3^{-2} \longrightarrow x = -2$

② $2 \log x - 1 = \log(x^2 - 6)$

$\log x^2 - \log 10 = \log(x^2 - 6) \longrightarrow \log \dfrac{x^2}{10} = \log(x^2 - 6) \longrightarrow \dfrac{x^2}{10} = x^2 - 6$

$x^2 = 10x^2 - 60 \longrightarrow 60 = 9x^2 \longrightarrow x = \pm\sqrt{\dfrac{60}{9}}$ Sólo vale $x = +\sqrt{\dfrac{60}{9}} = \dfrac{2\sqrt{15}}{3}$

③ $\left. \begin{array}{l} x - y = 3 \\ 2^x - 2^y = \frac{7}{4} \end{array} \right\} \quad x = 3 + y$

$2^{3+y} - 2^y = \dfrac{7}{4} \longrightarrow 2^3 \cdot 2^y - 2^y = \dfrac{7}{4} \xrightarrow{2^y = t}$

$8t - t = \dfrac{7}{4} \longrightarrow 7t = \dfrac{7}{4} \longrightarrow t = \dfrac{1}{4} \longrightarrow 2^y = \dfrac{1}{4} = 2^{-2} \longrightarrow y = -2$

$x = 3 - 2 = 1 \longrightarrow \boxed{\begin{array}{l} x = 1 \\ y = -2 \end{array}}$

④ $\log 2 = 0{,}3010 , \quad \log 3 = 0{,}4771 , \quad \log 5 = 0{,}6990$

a) $\log \sqrt[6]{\dfrac{1}{0{,}128}} = \log \sqrt[6]{\dfrac{125}{16}} = \dfrac{1}{6} \log \dfrac{125}{16} = \dfrac{1}{6}\left[\log 125 - \log 16\right] =$

$= \dfrac{1}{6}\left[\log 5^3 - \log 2^4\right] = \dfrac{1}{6}\left[3\log 5 - 4\log 2\right] =$

$= \dfrac{1}{6}\left[3 \cdot 0{,}6990 - 4 \cdot 0{,}3010\right] = 0{,}1488$

b) $\log \dfrac{540}{256} = \log \dfrac{2^2 \, 3^3 \, 5}{2^8} = \log 2^2 \cdot 3^3 \cdot 5 - \log 2^8 =$

$= 2\log 2 + 3\log 3 + \log 5 - 8 \cdot \log 2 = 0{,}3243$

⑤ $\log A = 2 + 5\log x + \dfrac{3}{5}\log y - 4\log z - 3\log \dfrac{x}{y}$

$\log A = \log 100 + \log x^5 + \log \sqrt[5]{y^3} - \log z^4 - \log\left(\dfrac{x}{y}\right)^3$

$A = \dfrac{100 \cdot x^5 \cdot \sqrt[5]{y^3}}{z^4 \cdot \dfrac{x^3}{y^3}} = \dfrac{100 \, x^2 \cdot y^3 \sqrt[5]{y^3}}{z^4}$

⑥ $\log x - \log y = 1$ ⎫ $\log \frac{x}{y} = \log 10$ ⎫ $x = 10y$

$3x + 2y = 64$ ⎭ $3x + 2y = 64$ ⎭ $3 \cdot 10y + 2y = 64$

$32y = 64$ — $\boxed{y = 2}$

$\boxed{x = 20}$

⑦. $\dfrac{\log 2 + \log (11 - x^2)}{\log (5 - x)} = 2$

$\log 2 + \log (11 - x^2) = 2 \log (5 - x)$

$\log 2 (11 - x^2) = \log (5 - x)^2$

$22 - 2x^2 = 25 - 10x + x^2$

$-3x^2 + 10x - 3 = 0$ ⟨ $x_1 = 3$

$x_2 = \dfrac{1}{3}$

⑧ $4^{1+x} + 2^{x+3} = 320$

$(2^2)^{1+x} + 2^{x+3} = 320 \longrightarrow 2^2 \cdot (2^x)^2 + 2^x \cdot 2^3 = 320 \rightarrow \boxed{2^x = t}$

$4t^2 + 8t - 320 = 0$ ⟨ $t_1 = 8 \longrightarrow 2^x = 8 \rightarrow x = 3$

$t_2 = -10 \rightarrow 2^x = -10$ ✗