## PROPORTION - PERCENTAGE - FRACTIONS

Name: $\qquad$

1) Calculate and simplify:
(3 points)
a) $\frac{2}{5}-\left(\frac{1}{2}+\frac{3}{5}\right) \times 2=$
b) $\frac{3}{5} \div \frac{6}{15}-\frac{4}{5} \div \frac{1}{3}=$
c) $\left(\frac{1}{7}+\frac{1}{3}\right) \times\left(\frac{1}{2}-\frac{3}{7}\right)=$
2) Write each ratio as a fraction, a decimal and a percent:
(1 point)

| RATIO | FRACTION | DECIMAL | PERCENT |
| :---: | :---: | :---: | :---: |
| 15 to 100 |  |  |  |
| 9 to 50 |  |  |  |
| 6 to 100 |  |  |  |
| 72 to 100 |  |  |  |

3) Find the value of $X$ :
(1 point)

| a) $30 \%$ of $X=36$ | b) $150 \%$ of $X=114$ |
| :--- | :--- |
| c) $74 \%$ of $X=111$ | d) $22 \%$ of $X=77$ |

4) There are 750 students at Murillo School. 135 students ride the bus to school. What percentage of the students do not ride the bus?
5) The price of a cinema ticket increases from 6 euros to 7.5 euros. What is the percentage of increase? (1 point)
6) If a farmer has enough cattle feed to feed 240 cows for 15 days. How long would the same food last for 360 cows? (1 point)

7) Rafael Nadal won $86 \%$ of his matches last year. If he won 80 matches in 2008, how many matches did he play?
(1 point)
8) Walter got a $15 \%$ discount when he bought his new jacket. If the original price, before the discount, was $€ 70$, how much was the discount?
(1 point)

## SOLUTIONS

1) a) $\frac{2}{5}-\left(\frac{1}{2}+\frac{3}{5}\right) \times 2=\frac{2}{5}-\frac{5+6}{10} \times 2=\frac{2}{5}-\frac{22}{10}=\frac{2}{5}-\frac{11}{5}=-\frac{9}{5}$
b) $\frac{3}{5} \div \frac{6}{15}-\frac{4}{5} \div \frac{1}{3}=\frac{3 \times 15}{5 \times 6}-\frac{4 \times 3}{5}=\frac{3}{2}-\frac{12}{5}=\frac{15}{10}-\frac{24}{10}=-\frac{9}{10}$
c) $\left(\frac{1}{7}+\frac{1}{3}\right) \times\left(\frac{1}{2}-\frac{3}{7}\right)=\frac{3+7}{21} \times \frac{7-6}{14}=\frac{10}{21} \times \frac{1}{14}=\frac{5}{147}$
2) Write each ratio as a fraction, a decimal and a percent:

| RATIO | FRACTION | DECIMAL | PERCENT |
| :---: | :---: | :---: | :---: |
| 15 to 100 | $\frac{15}{100}=\frac{3}{20}$ | 0.15 | $15 \%$ |
| 9 to 50 | $\frac{9}{50}$ | 0.18 | $18 \%$ |
| 6 to 100 | $\frac{6}{100}=\frac{3}{50}$ | 0.06 | $6 \%$ |
| 72 to 100 | $\frac{72}{100}=\frac{18}{25}$ | 0.72 | $72 \%$ |

3) Find the value of $X$ :

| a) $30 \%$ of $x=36$ <br> $\frac{30}{100}=\frac{36}{x} \rightarrow 30 x=3600 \rightarrow x=120$ | b) $150 \%$ of $x=114$ <br> $\frac{150}{100}=\frac{114}{x} \rightarrow 150 x=11400 \rightarrow x=76$ |
| :--- | :--- |
| c) $74 \%$ of $X=111$ <br> $\frac{74}{100}=\frac{111}{x} \rightarrow 74 x=11100 \rightarrow x=150$ | d) $22 \%$ of $X=77$ <br> $\frac{22}{100}=\frac{77}{x} \rightarrow 22 x=7700 \rightarrow x=350$ |

4) There are 750 students at Murillo School. 135 students ride the bus to school.

What percentage of the students do not ride the bus? $750-135=615$
750 ------ 615 DIRECT proportion $\frac{750}{100}=\frac{615}{x} \rightarrow 750 x=61500 \rightarrow x=82$ 100 $\qquad$
SOLUTION: $82 \%$ of the students do not ride the bus
5) The price of a cinema ticket increases from 6 euros to 7.5 euros. What is the percentage of increase?
$7.5-6=1.5$
6 $\qquad$

$$
\frac{6}{100}=\frac{1.5}{x} \rightarrow 6 x=150 \rightarrow x=25 \%
$$

$\qquad$ - $x$

SOLUTION: the percentage increases is $25 \%$
6) If a farmer has enough cattle feed to feed 240 cows for 15 days. How long would the same food last for 360 cows?
240 cows -------------- 15 days INVERSE proportion
360 cows $x$ days

$$
\begin{aligned}
& \frac{240}{360}=\frac{x}{15} \rightarrow 360 x=240 \times 15 \rightarrow 360 x=3600 \\
& x=3600 \div 360=10
\end{aligned}
$$



SOLUTION: The same food would last 10 days to feed 360 cows
7) Rafael Nadal won $86 \%$ of his matches last year. If he won 80 matches in 2008, how many matches did he play?
$86 \%$--------- 80 matches $\frac{86}{100}=\frac{80}{x} \rightarrow 86 x=8000 \rightarrow x=93.02$
100\% $\qquad$ $x$ matches

SOLUTION: Rafael Nadal played 93 matches in 2008
8) Walter got a $15 \%$ discount when he bought his new jacket. If the original price, before the discount, was $€ 70$, how much was the discount?
$15 \%$ of $70=\frac{15 \times 70}{100}=10.5$

SOLUTION: The discount was $€ 10.5$

