

EXAM 2_1 (FUNCTIONS/INEQUALITIES)

Name: _____

1. Plot the function: $f(x) = \begin{cases} 2-x & \text{if } x < -1 \\ 3 & \text{if } -1 < x \leq 3 \\ 2x-5 & \text{if } x > 3 \end{cases}$ (2p)

And find:

- Its domain and range.
- Continuity.
- Increasing and decreasing intervals.

2. Find the domain of the following functions: (2.25 p)

$$f(x) = \frac{x^3 + 3}{x^2 - 9x + 8}; \quad g(x) = \sqrt[3]{\frac{x}{x^2 - 1}}; \quad h(x) = \sqrt{\frac{x+1}{9-x^2}}$$

3. Given the equation of the parabola $f(x) = -x^2 + 4x - 3$ (1.5 p)

- Find its vertex and symmetry axis.
- Its intersections with the x axis and the y axis.
- Draw the graph of $f(x)$.
- Find the range of $f(x)$.

4. Solve by graphing the simultaneous equation: $\left. \begin{array}{l} y = x^2 - 2x \\ y = x + 4 \end{array} \right\}$ (2 p)

(Write the steps you have taken to reach the solution)

5. Solve the following systems of inequalities: (2.25 p)

$$\left. \begin{array}{l} \text{a) } \begin{cases} x + 2y \leq 10 \\ y > x - 2 \end{cases} \\ \text{b) } \begin{cases} 2(x+1) > x - 7 \\ \frac{2x-3}{3} \leq 2(x+1) - 1 \\ 2x - 5 < x - 5 \end{cases} \end{array} \right\}$$

